

q -Expansion of the square of the Vandermonde determinant

Factored form

The first entry in square brackets is the value of the q -polynomial for $q = 1$

$\mathbf{N} = 2$

$$\begin{aligned} & [1]q\{2\} \\ & [-3] - (q^2 + q + 1)\{1^2\} \end{aligned}$$

$\mathbf{N} = 3$

$$\begin{aligned} & [1]q^3\{42\} \\ & [-3] - q^2(q^2 + q + 1)(\{41^2\} + \{3^2\}) \\ & [6] + q(q^2 + q + 1)(q^2 + 1)\{321\} \\ & [-15] - (q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)\{2^3\} \end{aligned}$$

$\mathbf{N} = 4$

$$\begin{aligned} & [1]q^6\{642\} \\ & [-3] - q^5(q^2 + q + 1)(\{641^2\} + \{63^2\} + \{5^22\}) \\ & [6] + q^4(q^2 + 1)(q^2 + q + 1)(\{6321\} + \{543\}) \\ & [9] + q^4(q^2 + q + 1)^2\{5^21^2\} \\ & [-15] - q^3(q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(\{62^3\} + \{4^3\}) \\ & [-12] - q^3(q^2 + q + 1)(q^2 + 1)^2\{5421\} \\ & [-9] - q^3(q^2 - q + 1)(q^2 + q + 1)^2\{53^21\} \\ & [-6] - q^3(q^2 + q + 1)(q^4 + 1)\{4^22^2\} \\ & [27] + q^2(q^2 - q + 1)(q^2 + q + 1)^3(\{532^2\} + \{4^231\}) \\ & [-45] - q(q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2\{43^22\} \\ & [105] + (q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)\{3^4\} \end{aligned}$$

$$\begin{aligned}
& [1]q^{10}\{8642\} \\
& [-3] - q^9(q^2 + q + 1)(\{8641^2\} + \{863^2\} + \{85^22\} + \{7^242\}) \\
& [6] + q^8(q^2 + 1)(q^2 + q + 1)(\{86321\} + \{8543\} + \{7652\}) \\
& [9] + q^8(q^2 + q + 1)^2(\{85^21^2\} + \{7^241^2\} + \{7^23^2\}) \\
& [-12] - q^7(q^2 + q + 1)(q^2 + 1)^2(\{85421\} + \{7643\}) \\
& [-9] - q^7(q^2 - q + 1)(q^2 + q + 1)^2(\{853^21\} + \{75^23\}) \\
& [-6] - q^7(q^2 + q + 1)(q^4 + 1)(\{84^22^2\} + \{6^24^2\}) \\
& [-15] - q^7(q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(\{862^3\} + \{84^3\} + \{6^32\}) \\
& [-18] - q^7(q^2 + 1)(q^2 + q + 1)^2(\{7^2321\} + \{7651^2\}) \\
& [27] + q^6(q^2 - q + 1)(q^2 + q + 1)^3(\{8532^2\} + \{84^231\} + \{754^2\} + \{6^253\}) \\
& [24] + q^6(q^2 + q + 1)(q^2 + 1)^3\{76421\} \\
& [18] + q^6(q^2 + 1)(q^2 - q + 1)(q^2 + q + 1)^2(\{763^21\} + \{75^221\}) \\
& [45] + q^6(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{7^22^3\} + \{6^31^2\}) \\
& [-45] - q^5(q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{843^22\} + \{65^24\}) \\
& [-54] - q^5(q^2 + 1)(q^2 - q + 1)(q^2 + q + 1)^3(\{7632^2\} + \{6^2521\}) \\
& [-36] - q^5(q^2 - q + 1)(q^2 + q + 1)^2(q^2 + 1)^2(\{75431\} + \{74^31\}) \\
& [-27] - q^5(q^2 - q + 1)^2(q^2 + q + 1)^3(\{7542^2\} + \{6^2431\}) \\
& [-18] - q^5(q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^2(\{6^23^22\} + \{65^22^2\}) \\
& [105] + q^4(q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(\{83^4\} + \{5^4\}) \\
& [16] + q^4(q^2 - q + 1)^2(q^2 + q + 1)^4(\{753^22\} + \{65^231\}) \\
& [72] + q^4(q^4 + 1)(q^2 + 1)^2(q^2 + q + 1)^2(\{74^232\} + \{654^21\}) \\
& [111] + q^4(q^2 + q + 1)(q^{10} + 2q^9 + 4q^8 + 3q^7 + 6q^6 + 5q^5 + 6q^4 + 3q^3 + 4q^2 + 2q + 1)\{6^242^2\} \\
& [54] + q^4(q^4 - q^3 + q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{653^3\} + \{5^332\}) \\
& [-180] - q^3(q^2 + 1)(q^4 + q^3 + q^2 + q + 1)(q^4 + 1)(q^2 + q + 1)^2(\{743^3\} + \{5^341\}) \\
& [-144] - q^3(q^4 + 1)(q^2 + q + 1)^2(q^2 + 1)^3\{65432\} \\
& [-90] - q^3(q^4 + q^3 + q^2 + q + 1)(q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^2\{64^32\} \\
& [-75] - q^3(q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)^2\{5^243^2\} \\
& [270] + q^2(q^4 + q^3 + q^2 + q + 1)(q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^3(\{64^23^2\} + \{5^24^22\}) \\
& [-420] - q(q^2 + q + 1)(q^2 + 1)(q^4 + q^3 + q^2 + q + 1)(q^4 + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)\{54^33\} \\
& [945] + (q^4 + q^3 + q^2 + q + 1)(q^6 + q^3 + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2\{4^5\}
\end{aligned}$$

$$\begin{aligned}
& [1]q^{15}\{10\ 8642\} \\
& [-3] - q^{14}(q^2 + q + 1)(\{10\ 8641^2\} + \{10\ 863^2\} + \{10\ 85^2 2\} + \{10\ 7^2 42\} + \{9^2 642\}) \\
& [6] + q^{13}(q^2 + q + 1)(q^2 + 1)(\{10\ 86321\} + \{10\ 8543\} + \{10\ 7652\} + \{98742\}) \\
& [9] + q^{13}(q^2 + q + 1)^2(\{10\ 85^2 1^2\} + \{10\ 7^2 41^2\} + \{10\ 7^2 3^2\} + \{9^2 641^2\} + \{9^2 63^2\} + \{9^2 5^2 2\}) \\
& [-15] - q^{12}(q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(\{10\ 862^3\} + \{10\ 84^3\} + \{10\ 6^3 2\} + \{8^3 42\}) \\
& [-9] - q^{12}(q^2 - q + 1)(q^2 + q + 1)^2(\{10\ 853^2 1\} + \{10\ 75^2 3\} + \{97^2 52\}) \\
& [-12] - q^{12}(q^2 + q + 1)(q^2 + 1)^2(\{10\ 85421\} + \{10\ 7643\} + \{98652\}) \\
& [-6] - q^{12}(q^2 + q + 1)(q^4 + 1)(\{10\ 84^2 2^2\} + \{10\ 6^2 4^2\} + \{8^2 6^2 2\}) \\
& [-18] - q^{12}(q^2 + 1)(q^2 + q + 1)^2(\{10\ 7^2 321\} + \{10\ 7651^2\} + \{9^2 6321\} + \{9^2 543\} + \{98741^2\} + \{9873^2\}) \\
& [-27] - q^{12}(q^2 + q + 1)^3\{9^2 5^2 1^2\} \\
& [27] + q^{11}(q^2 - q + 1)(q^2 + q + 1)^3(\{10\ 8532^2\} + \{10\ 84^2 31\} + \{10\ 754^2\} + \{10\ 6^2 53\} \\
& \quad + \{9^2 53^2 1\} + \{97^2 51^2\} + \{976^2 2\} + \{8^2 752\}) \\
& [24] + q^{11}(q^2 + q + 1)(q^2 + 1)^3(\{10\ 76421\} + \{98643\}) \\
& [45] + q^{11}(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{10\ 7^2 2^3\} + \{10\ 6^3 1^2\} \\
& \quad + \{9^2 62^3\} + \{9^2 4^3\} + \{8^3 41^2\} + \{8^3 3^2\}) \\
& [18] + q^{11}(q^2 - q + 1)(q^2 + 1)(q^2 + q + 1)^2(\{10\ 763^2 1\} + \{10\ 75^2 21\} + \{985^2 3\} + \{97^2 43\}) \\
& [36] + q^{11}(q^2 + 1)^2(q^2 + q + 1)^2(\{9^2 5421\} + \{987321\}) + \{98651^2\}) \\
& [18] + q^{11}(q^4 + 1)(q^2 + q + 1)^2(\{9^2 4^2 2^2\} + \{8^2 6^2 1^2\}) \\
& [-36] - q^{10}(q^2 + 1)(q^4 + 1)(q^2 + q + 1)^2(\{10\ 74^3 1\} + \{96^3 3\}) \\
& [-45] - q^{10}(q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{10\ 843^2 2\} + \{10\ 65^2 4\} + \{87^2 62\}) \\
& [-54] - q^{10}(q^2 - q + 1)(q^2 + 1)(q^2 + q + 1)^3(\{10\ 7632^2\} + \{10\ 6^2 521\} + \{9854^2\} + \{8^2 743\}) \\
& [-36] - q^{10}(q^2 - q + 1)(q^2 + 1)^2(q^2 + q + 1)^2(\{10\ 75431\} + \{9863^2 1\} + \{985^2 21\} + \{97^2 421\} + \{97653\}) \\
& [-27] - q^{10}(q^2 - q + 1)^2(q^2 + q + 1)^3(\{10\ 7542^2\} + \{10\ 6^2 431\} + \{97^2 3^2 1\} + \{9764^2\} + \{8^2 653\}) \\
& [-18] - q^{10}(q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^2(\{10\ 6^2 3^2 2\} + \{10\ 65^2 2^2\} + \{8^2 5^2 4\} + \{87^2 4^2\}) \\
& [-81] - q^{10}(q^2 - q + 1)(q^2 + q + 1)^4(\{9^3 532^2\} + \{9^2 4^2 31\} + \{976^2 1^2\} + \{8^2 751^2\}) \\
& [-90] - q^{10}(q^2 + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{9872^3\} + \{8^3 321\}) \\
& [-48] - q^{10}(q^2 + q + 1)(q^2 + 1)^4\{986421\} \\
& [105] + q^9(q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(\{10\ 83^4\} + \{10\ 5^4\} + \{7^4 2\}) \\
& [81] + q^9(q^2 - q + 1)^2(q^2 + q + 1)^4(\{10\ 753^2 2\} + \{10\ 65^2 31\} + \{97^2 32^2\} + \{975^2 4\} + \{8^2 73^2 1\} + \{87^2 53\}) \\
& [72] + q^9(q^4 + 1)(q^2 + 1)^2(q^2 + q + 1)^2(\{10\ 74^2 32\} + \{10\ 654^2 1\} + \{984^3 1\} \\
& \quad + \{96^3 21\} + \{96^2 54\} + \{876^2 3\}) \\
& [111] + q^9(q^2 + q + 1)(q^{10} + 2q^9 + 4q^8 + 3q^7 + 6q^6 + 5q^5 + 6q^4 + 3q^3 + 4q^2 + 2q + 1)(\{10\ 6^2 42^2\} + \{8^2 64^2\}) \\
& [45] + q^9(q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(q^2 + q + 1)^2(\{10\ 653^3\} + \{10\ 5^3 32\} + \{875^3\} + \{7^3 54\}) \\
& [135] + q^9(q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^3(\{9^2 43^2 2\} + \{87^2 61^2\}) \\
& [108] + q^9(q^2 - q + 1)(q^2 + 1)^2(q^2 + q + 1)^3(\{98632^2\} + \{8^2 7421\}) \\
& [72] + q^9(q^2 - q + 1)(q^2 + q + 1)^2(q^2 + 1)^3(\{985431\} + \{976521\}) \\
& [54] + q^9(q^2 + 1)(q^2 - q + 1)^2(q^2 + q + 1)^3(\{98542^2\} + \{8^2 6521\}) \\
& [99] + q^9(q^2 - q + 1)(q^2 + q + 1)^2(2q^6 + 4q^4 - q^3 + 4q^2 + 2)\{976431\}
\end{aligned}$$

$$\begin{aligned}
& [81] + q^9(q^2 - q + 1)(q^2 + q + 1)^4(2q^2 - 3q + 2)(\{975^2 2^2\} + \{8^2 5^2 31\}) \\
& [225] + q^9(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)^2\{8^3 2^3\} \\
[-180] & - q^8(q^2 + 1)(q^4 + q^3 + q^2 + q + 1)(q^4 + 1)(q^2 + q + 1)^2(\{10\ 743^3\} + \{10\ 5^3 41\} + \{965^3\} + \{7^3 63\}) \\
[-144] & - q^8(q^4 + 1)(q^2 + q + 1)^2(q^2 + 1)^3(\{10\ 65432\} + \{984^2 32\} + \{876^2 21\} + \{87654\}) \\
[-90] & - q^8(q^4 + q^3 + q^2 + q + 1)(q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^2(\{10\ 64^3 2\} + \{86^3 4\}) \\
[-75] & - q^8(q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)^2(\{10\ 5^2 43^2\} + \{7^2 65^2\}) \\
[-315] & - q^8(q^4 + q^3 + q^2 + q + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{9^2 3^4\} + \{7^4 1^2\}) \\
[-162] & - q^8(q^2 + 1)(q^2 - q + 1)^2(q^2 + q + 1)^4(\{9853^2 2\} + \{87^2 521\}) \\
[-162] & - q^8(q^2 + q + 1)^3(q^2 - q + 1)(q^6 + 3q^4 - 2q^3 + 3q^2 + 1)(\{97642^2\} + \{975^2 31\} + \{8^2 6431\}) \\
[-81] & - q^8(q^2 + q + 1)^4(q^2 - q + 1)^3(\{9763^2 2\} + \{9754^2 1\} + \{96^2 531\} + \{87^2 431\}) \\
[-117] & - q^8(q^2 + q + 1)^2(q^{10} + 3q^8 - q^7 + 4q^6 - q^5 + 4q^4 - q^3 + 3q^2 + 1)(\{96^2 52^2\} + \{96^2 4^2 1\} + \{8^2 54^2 1\}) \\
[-81] & - q^8(q^2 + q + 1)^3(q^8 - q^7 + 2q^6 - q^5 + q^4 - q^3 + 2q^2 - q + 1)(\{96^2 3^3\} + \{7^3 4^2 1\}) \\
[-243] & - q^8(q^2 + q + 1)^5(q^2 - q + 1)^2\{8^2 732^2\} \\
[-69] & - q^8(q^2 + q + 1)(q^{12} + 2q^{10} + 6q^8 + 5q^6 + 6q^4 + 2q^2 + 1)\{8^2 642^2\} \\
[-153] & - q^8(q^2 - q + 1)(q^2 + q + 1)^2(q^8 + 2q^7 + 4q^6 + q^5 + q^4 + q^3 + 4q^2 + 2q + 1)\{8^2 5^2 2^2\} \\
[-36] & - q^8(q^2 - q + 1)(q^2 + q + 1)^2(q^4 + 1)^2(\{8^2 4^3 2\} + \{86^3 2^2\}) \\
[-54] & - q^8(q^2 - q + 1)^2(q^2 + q + 1)^3(q^4 + 1)\{87^2 3^2 2\} \\
[-90] & - q^8(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)(q^6 + q^4 - 2q^3 + q^2 + 1)\{7^3 3^3\} \\
[270] & + q^7(q^4 + q^3 + q^2 + q + 1)(q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^3(\{10\ 64^2 3^2\} + \{10\ 5^2 4^2 2\} + \{86^2 5^2\}) \\
[360] & + q^7(q^4 + q^3 + q^2 + q + 1)(q^4 + 1)(q^2 + q + 1)^2(q^2 + 1)^2(\{9843^3\} + \{7^3 621\}) \\
[270] & + q^7(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^3(q^2 - q + 1)(q^4 + 1)\{7^2 6^2 4\} \\
[162] & + q^7(q^2 + 1)(q^2 - q + 1)^3(q^2 + q + 1)^4(\{975432\} + \{876531\}) \\
[162] & + q^7(q^4 + 1)(q^2 - q + 1)^2(q^2 + q + 1)^4(\{9753^3\} + \{974^3 2\} + \{86^3 31\} + \{7^3 531\}) \\
[234] & + q^7(q^2 + 1)(q^2 + q + 1)^2(q^{10} + 3q^8 - q^7 + 4q^6 - q^5 + 4q^4 - q^3 + 3q^2 + 1)(\{96^2 432\} + \{8^2 5432\} + \{87652^2\} + \{8764^2 1\}) \\
[216] & + q^7(q^2 + 1)^2(q^4 + 1)(q^2 - q + 1)(q^2 + q + 1)^3\{965^2 41\} \\
[108] & + q^7(q^2 + 1)(q^4 + 1)(q^2 - q + 1)^2(q^2 + q + 1)^3(\{965^2 32\} + \{875^2 41\}) \\
[225] & + q^7(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)^2(q^4 - q^3 + q^2 - q + 1)\{95^4 1\} \\
[90] & + q^7(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(q^4 + 1)(\{95^3 3^2\} + \{7^2 5^3 1\}) \\
[45] & + q^7(q^2 + q + 1)^2(q^4 - q^2 + 1)(q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(\{7^2 4^4\} + \{6^4 3^2\}) \\
[333] & + q^7(q^2 + q + 1)^2(q^2 - q + 1)(q^{10} + 2q^9 + 4q^8 + 3q^7 + 6q^6 + 5q^5 + 6q^4 + 3q^3 + 4q^2 + 2q + 1)(\{8^2 63^2 2\} + \{87^2 42^2\}) \\
[108] & + q^7(q^2 + q + 1)^3(q^2 - q + 1)(q^4 + 1)^2(\{8^2 4^2 3^2\} + \{7^2 6^2 2^2\}) \\
[162] & + q^7(q^2 + 1)(q^2 + q + 1)^3(q^8 - q^7 + 2q^6 - q^5 + q^4 - q^3 + 2q^2 - q + 1)(\{8763^3\} + \{7^3 432\}) \\
[-420] & - q^6(q^2 + q + 1)(q^2 + 1)(q^4 + q^3 + q^2 + q + 1)(q^4 + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(\{10\ 54^3 3\} + \{76^3 5\}) \\
[-486] & - q^6(q^2 + q + 1)^5(q^2 - q + 1)^2(q^4 + 1)(\{974^2 3^2\} + \{7^2 6^2 31\}) \\
[-324] & - q^6(q^2 + q + 1)^4(q^2 - q + 1)^2(q^4 + 1)(q^2 + 1)(\{9654^2 2\} + \{86^2 541\}) \\
[-405] & - q^6(q^2 - q + 1)(q^2 + q + 1)^4(q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(\{95^3 42\} + \{865^3 1\}) \\
[-711] & - q^6(q^2 + q + 1)^2(q^{14} + 2q^{13} + 4q^{12} + 4q^{11} + 8q^{10} + 7q^9 + 10q^8 + 7q^7 + 10q^6 + 7q^5 + 8q^4 + 4q^3 + 4q^2 + 2q + 1) \\
& (\{8^2 53^3\} + \{7^3 52^2\}) \\
[-468] & - q^6(q^2 + 1)^2(q^2 + q + 1)^2(q^{10} + 3q^8 - q^7 + 4q^6 - q^5 + 4q^4 - q^3 + 3q^2 + 1)\{876432\} \\
[-351] & - q^6(q^2 - q + 1)(q^2 + q + 1)^3(q^{10} + 3q^8 - q^7 + 4q^6 - q^5 + 4q^4 - q^3 + 3q^2 + 1)\{875^2 32\} \\
[-201] & - q^6(q^2 + q + 1)(q^{16} + q^{15} + 4q^{14} + 2q^{13} + 6q^{12} + 3q^{11} + 9q^{10} \\
& + 3q^9 + 9q^8 + 3q^7 + 9q^6 + 3q^5 + 6q^4 + 2q^3 + 4q^2 + q + 1)\{7^2 643^2\}
\end{aligned}$$

$$\begin{aligned}
& [-162] - q^6(q^4 + 1)(q^2 - q + 1)^3(q^2 + q + 1)^4(\{8754^22\} + \{86^2532\}) \\
& [-108] - q^6(q^4 + 1)^2(q^2 - q + 1)^2(q^2 + q + 1)^3(\{86^243^2\} + \{7^264^22\}) \\
& [-288] - q^6(q^4 + 1)^2(q^2 + q + 1)^2(q^2 + 1)^3(\{96543^2\} + \{7^26541\}) \\
& [-180] - q^6(q^2 + 1)(q^4 + 1)(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)\{76^332\} \\
& [945] + q^5(q^4 + q^3 + q^2 + q + 1)(q^6 + q^3 + 1)(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(\{10\ 4^5\} + \{6^5\}) \\
& [720] + q^5(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(q^4 + 1)^2(q^2 + 1)^2(\{964^33\} + \{76^341\}) \\
& [675] + q^5(q^4 + q^3 + q^2 + q + 1)^2(q^4 - q^3 + q^2 - q + 1)(q^2 + q + 1)^3(q^2 - q + 1)(\{95^24^23\} + \{76^25^21\}) \\
& [801] + q^5(q^2 + q + 1)^2(q^{16} + q^{15} + 4q^{14} + 2q^{13} + 9q^{12} + 3q^{11} + 13q^{10} \\
& \quad + 4q^9 + 15q^8 + 4q^7 + 13q^6 + 3q^5 + 9q^4 + 2q^3 + 4q^2 + q + 1)(\{87543^2\} + \{7^26532\}) \\
& [666] + q^5(q^4 + 1)(q^2 + q + 1)^2(q^{10} + 2q^9 + 4q^8 + 3q^7 + 6q^6 + 5q^5 + 6q^4 + 3q^3 + 4q^2 + 2q + 1)\{86^24^22\} \\
& [567] + q^5(q^2 + q + 1)^3(q^2 - q + 1)(q^{12} + 3q^{10} + q^9 + 3q^8 + 5q^6 + 3q^4 + q^3 + 3q^2 + 1)\{865^242\} \\
& [324] + q^5(q^4 + 1)^2(q^2 - q + 1)^2(q^2 + q + 1)^4(\{865^23^2\} + \{7^25^242\}) \\
& [405] + q^5(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^4(q^2 - q + 1)^2(q^4 - q^2 + 1)(\{864^4\} + \{6^442\}) \\
& [450] + q^5(q^4 + q^3 + q^2 + q + 1)^2(q^4 - q^3 + q^2 - q + 1)(q^2 + q + 1)^2(q^4 + 1)\{85^42\} \\
& [270] + q^5(q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(q^4 + 1)(q^2 - q + 1)(q^2 + q + 1)^3(\{7^254^23\} + \{76^253^2\}) \\
& [345] + q^5(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)(q^{14} + 3q^{12} + 4q^{10} - q^9 + 5q^8 - q^7 + 5q^6 - q^5 + 4q^4 + 3q^2 + 1)\{76^24^23\} \\
& [225] + q^5(q^4 - q^3 + q^2 - q + 1)(q^4 - q^2 + 1)(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)\{6^34^3\} \\
& [-1575] - q^4(q^4 + q^3 + q^2 + q + 1)^2(q^4 - q^3 + q^2 - q + 1)(q^2 + q + 1)^2(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(\{954^4\} + \{6^451\}) \\
& [-900] - q^4(q^4 + q^3 + q^2 + q + 1)^2(q^4 - q^3 + q^2 - q + 1)(q^2 + q + 1)^2(q^2 + 1)(q^4 + 1)(\{85^343\} + \{765^32\}) \\
& [-1215] - q^4(q^4 - q^3 + q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^5(q^2 - q + 1)^2(\{8654^23\} + \{76^2542\}) \\
& [-1422] - q^4(q^4 + 1)(q^2 + q + 1)^2(q^{14} + 2q^{13} + 4q^{12} + 4q^{11} + 8q^{10} + 7q^9 + 10q^8 + 7q^7 + 10q^6 + 7q^5 + 8q^4 + 4q^3 + 4q^2 + 2q + 1) \\
& \quad \{7^25^23^2\} \\
& [-720] - q^4(q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2(q^4 + 1)(q^2 + 1)^3(q^4 - q^2 + 1)(\{7654^3\} + \{6^3543\}) \\
& [2250] + q^3(q^4 - q^3 + q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)^3(q^4 + 1)(q^2 + q + 1)^2(\{85^24^3\} + \{6^35^22\}) \\
& [1800] + q^3(q^4 - q^3 + q^2 - q + 1)(q^4 + q^3 + q^2 + q + 1)^2(q^4 + 1)(q^2 + q + 1)^2(q^2 + 1)^2\{765^243\} \\
& [1050] + q^3(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)^2(q^2 + q + 1)(q^4 + 1)(q^4 - q^3 + q^2 - q + 1)\{75^43\} \\
& [945] + q^3(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^4 + q^3 + q^2 + q + 1)(q^4 - q^2 + 1)(q^2 + q + 1)^3(q^2 - q + 1)^2\{6^25^24^2\} \\
& [-3150] - q^2(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^4 - q^3 + q^2 - q + 1)(q^4 + 1)(q^2 + q + 1)^2(q^4 + q^3 + q^2 + q + 1)^2 \\
& \quad (\{75^34^2\} + \{6^25^33\}) \\
& [4725] + q(q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^6 + q^3 + 1)(q^4 + q^3 + q^2 + q + 1)^2(q^2 + q + 1)^2\{65^44\} \\
& [-10395] - (q^4 + q^3 + q^2 + q + 1)(q^6 + q^3 + 1)(q^{10} + q^9 + q^8 + q^7 + q^6 + q^5 + q^4 + q^3 + q^2 + q + 1) \\
& \quad (q^6 + q^5 + q^4 + q^3 + q^2 + q + 1)(q^2 + q + 1)^2\{5^6\}
\end{aligned}$$